More triangle geometry

- 1. You should be able to construct all 4 triangle centers (Centroid, Orthocenter, Circumcenter, Incenter).
- 2. Describe or define Feuerbach circle.
- 3. You should be comfortable using the trace and locus tools in GeoGebra. Explain how you can draw a Feuerbach circle as a locus of (a) certain point(s).
- 4. Triangle ABC has the orthocenter O. What is the orthocenter of the triangle ABO? Prove it.
- 5. Triangle ABC has the orthocenter O. Describe the relationship between the Feuerbach circle of ABC and Feuerbach circle of BCO. Prove your answer.

1. Construct all 4 triangle centers

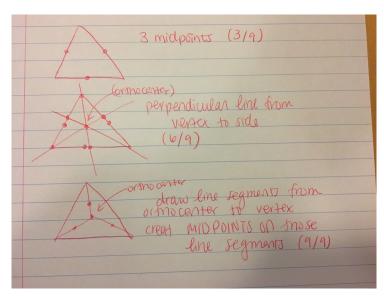
In order to create a centroid, create polygon with three points. Find midpoints of all three sides, connect midpoint to opposite vertex of triangle. medians.

Orthocenter - where all altitudes cross - can be inside of outsider

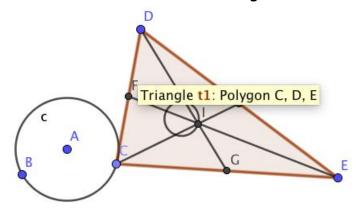
- i. Create perpendicular line from vertex to opposite side
 Circumcenter make midpoint on each side and create perpendicular line on midpoints intersection of perpendicular lines can be inside or outside
- Feuerbach Circle create triangle then make orthocenter and circumcircle, then find midpoint from orthocenter to circumcircle, then trace from midpoint to circumcircle. The circle that is traced is the feuerbach circle.
 9 point circle 3 midpoints from side lengths, 3 feet of altitudes and 3 midpoints from orthocenter to vertice.

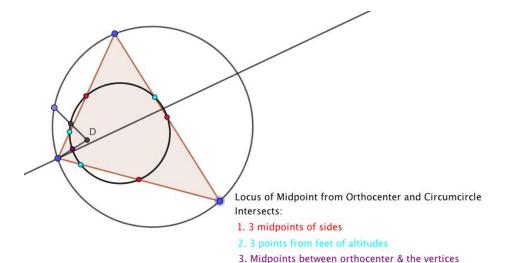
Create triangle and midpoint of each side (3/9 points are these midpoints)
Create perpendicular line from each vertex to opposite side (orthocenter)

- i. Create points where altitude and triangle sides intersect
 Create line from vertex to orthocenter and create midpoint of that line segment
 Extra information not discussed in class:
 - ii. Create circumcenter by create perpendicular line from midpoints of triangle
 - iii. Create line segment between orthocenter and circumcenter, find midpoint of that segment THIS IS center of circle



- 3. Explain how you can draw a Feuerbach circle as a locus of certain points create triangle then make orthocenter and circumcircle, then find midpoint from orthocenter to circumcircle, then trace from midpoint to circumcircle. The circle that is traced is the feuerbach circle.
 - 4. What is the orthocenter of the triangle ABO? The orthocenters are vertices



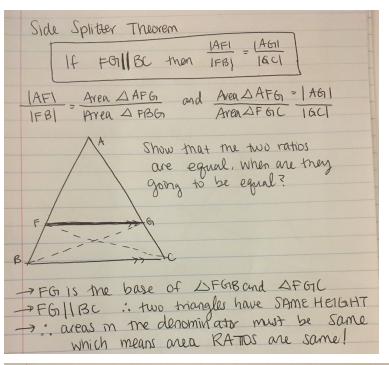


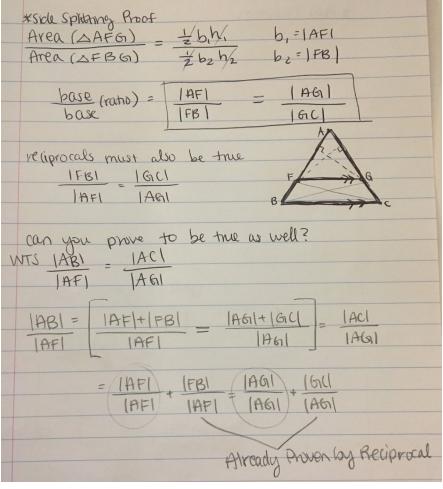
5. Describe relationship Geogebra File

Triangle similarity conditions

- 6. Discuss the difference between the definition of polygon similarity and similarity of general "figures".
- 7. Define similar triangles.
- 8. List triangle similarity conditions.
- 9. Formulate and prove the Side-splitter theorem. https://www.geogebra.org/m/PdGTJvDC
- 10. Formulate and prove corollary to the Side-splitter theorem.
- 11. Briefly discuss the importance of the Side-splitter theorem (and/or its corollary).
- 12. Prove the aa triangle similarity condition. https://www.geogebra.org/m/WT6nJZ6V
- 13. Using the aa similarity theorem and side-splitter theorem, outline the idea of the proof of sas similarity theorem (you don't have to prove it, just outline the idea).
- 6. For general blob two shapes are similar when there is one to one correspondence for any two pairs of line segment ratios check all such pairs in order to say that they are similar this definition is conceptual because it gives us an idea but it is not practical
 - a. When you have a blob you look at one to one ratio
- Similar Triangles have equal corresponding angles and proportional side lengths.
- 8. AA, SAS and SSS, ASA?

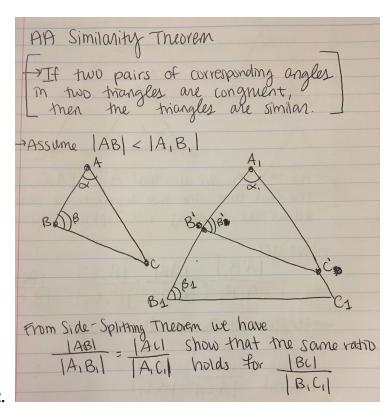
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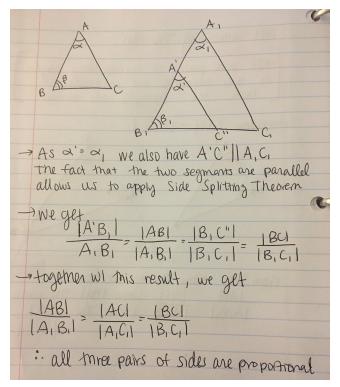


10. The bottom of the above photo is the corollary

11. Helps to prove triangle similarity theorems. Ex: AA



12.



13.

Triangle similarity applications

- 14. Formulate and prove Euclid's theorems about the height and legs in a right triangle. https://www.geogebra.org/m/tUYgVpRT
- 15. Use the previous result to prove the Pythagorean theorem.
- 16. The altitude to the hypotenuse of a right triangle is the geometric mean of the segments into which the altitude divides the hypotenuse. Try to make sense of what the theorem is saying. Draw a picture to explain it. Prove the theorem.

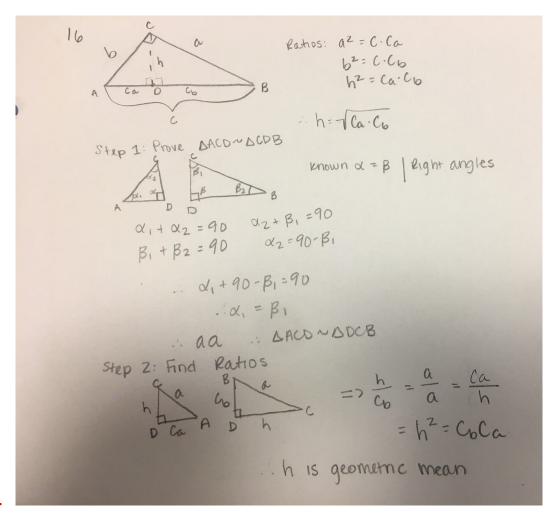
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h2 = Ca · Cb | Euclid's Theorem AABC~ACBD $\frac{a}{a} \times \frac{c}{a} \times \frac{c}{a}$ $\left[a^{2} - ca \cdot c\right]$ DABC ~ DADC $\frac{a}{b} = \frac{b}{c_b} = \frac{c}{b}$ b2 = (Cb) use $C^2 = C \cdot Ca$ $b^2 = C \cdot Ca$ $b^2 = (a \cdot Cb)$ to prove $C^2 = a^2 + b^2$ $b^2 = (a \cdot Cb)$

Proving Pythagoreon Theorem:

Known
$$C = CatCb$$
 $a^2 + b^2 = Cca + CCb$
 $a^2 + b^2 = C(ca + Cb)$
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 $a^2 + b^2 = C \cdot c$

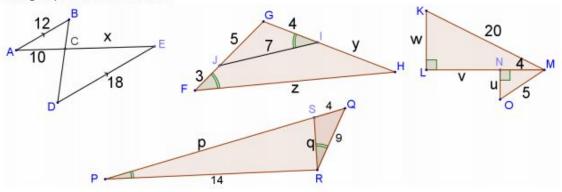
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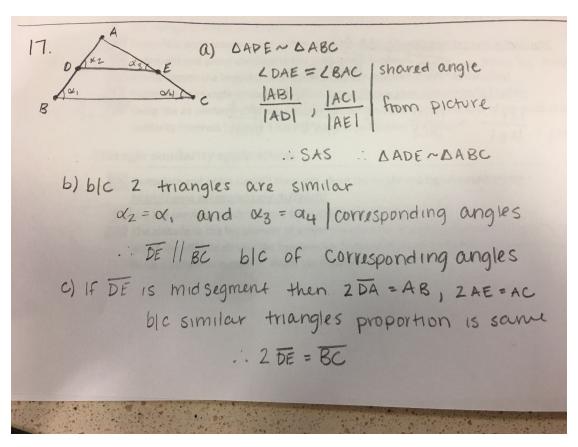
- 17. D is the midpoint of AB, E is the midpoint of AC. (See the picture; The segment DE is called *midsegment*.).
 - Identify similar triangles in the picture and provide proper justification.
 - b. DE | BC. Prove it.
 - c. 2x | DE | = | BC | . Prove it.

If you need hints, go to: https://www.geogebra.org/m/TeXKJjVc

- 18. Using the same triangle ABC and points D, E:
 - a. Show that F is the centroid of ABC.
 - b. Identify similar triangles in the picture (justify your selection) that will help you prove that the Centroid splits medians in the 2:1 ratio. More specifically, prove that: 2x|DF| = |FC|. If you need hints, go to (copy-paste the link to browser if clicking does not help): https://www.geogebra.org/m/ScZJ3mqC
- 19. Use triangle similarity to solve for the missing dimensions. Don't forget to justify why the triangles you chose are similar.

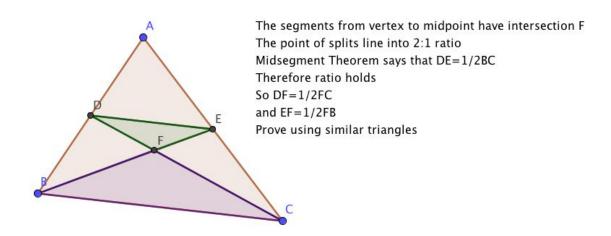


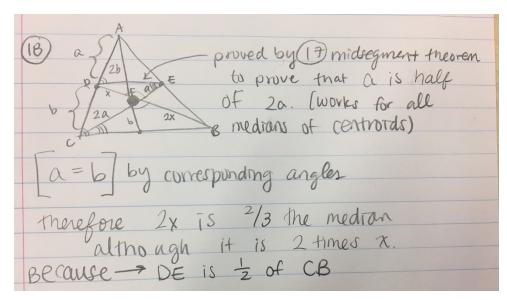
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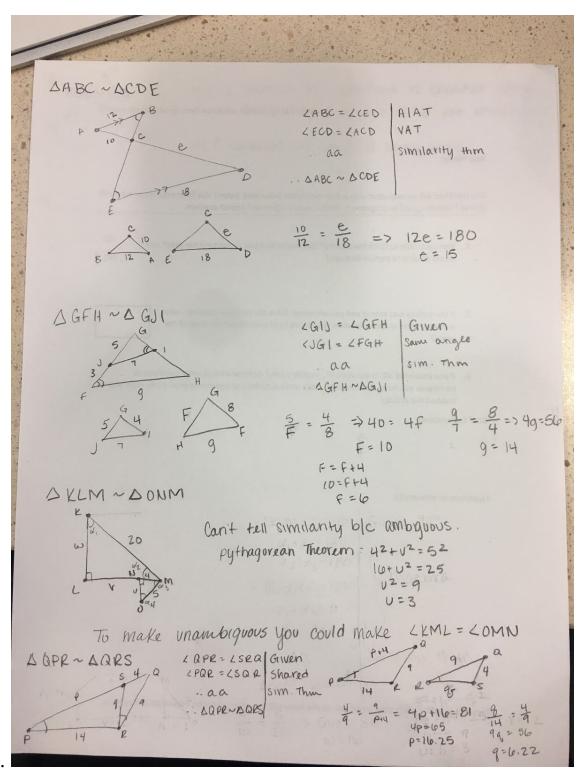
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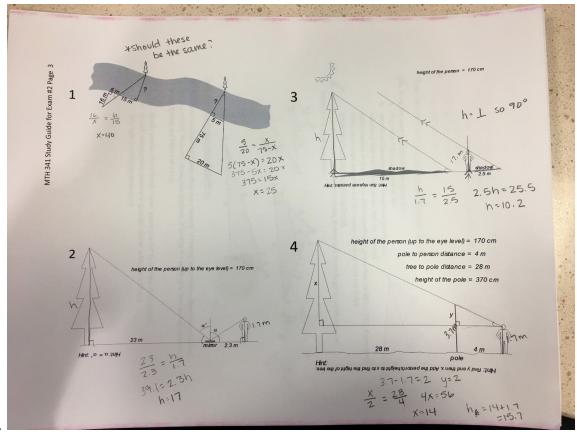
a.





b.





20.

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