## PABSON

SEE PRE BOARD EXAM - 2077 (PC231)
Time: 3:00 hrs Optional Mathematics
F.M. : 100

Candidates are required to write their answers according to the instructions given.
Attempt all questions.

## Group" A"

$5 \times(1+1)=10$

1. (a) Define constant function with an example.
(b) If $3, a, 27$ and 81 are in G.P., find the value of $a$.
2. (a) What is the point of discontinuity of a function $f(x)=$ $\frac{x+1}{x-1}$ ?
(b) Find the value of $k$ if $\left|\begin{array}{cc}4 & 1+k \\ 6 & 5\end{array}\right|=\left|\begin{array}{ll}2 & 4 \\ k & 3\end{array}\right|$
3. (a) If the lines $a_{1} x+b_{1} y+c_{1}=0$ and $a_{2} x+b_{2} y+c_{2}=0$ are parallel to each other, then show that $a_{1} b_{2}=a_{2} b_{1}$.
(b) If the intersection plane is parallel to the axis of cone then what conic does it form?
4. (a) Write the formula for $2 \sin A \cdot \sin B$.
(b) Solve: $3 \tan ^{2} \theta-1=0\left[0^{\circ} \leq \theta \leq 90^{\circ}\right]$
5. (a) If $\vec{a}=\vec{i}-2 \vec{j}$ and $\vec{b}=-6 \vec{i}-3 \vec{j}$, then prove that $\vec{a}$ is perpendicular to $\vec{b}$.
(b) If a point $P(-4,3 a-5)$ has its image $P^{\prime}(7-a, 4)$ under the reflection in the line $y=-x$, find the value of $a$.

## Group"B"

$[13 \times 2=26]$
6. (a) If $g(x+5)=x+20$ then find $g(x)$ and $\operatorname{gog}(x)$.
(b) If $x-\sqrt{2}$ is a factor of $a x^{3}-6 x+2 \sqrt{2}$, then find the value of $a$.
(c) What is the common difference of an AP whose first term and sum of first 15 terms are 100 and 450 respectively?
7. (a) If $P=\left[\begin{array}{cc}2 & -1 \\ -4 & 5\end{array}\right]$ and $Q=\left[\begin{array}{c}-3 \\ 3\end{array}\right]$, find the matrix $R$ such that $P R=Q$.
(b) According to Cramer's rule, find the values of $D_{x}$ and $D_{y}$ for $x+y=5$ and $x-y=3$.
8. (a) If the acute angle between two straight lines $2 x-y+6=0$ and $3 x+k y+4=0$ is $45^{\circ}$, find the value of $k$.
(b) Show that the lines $y+\sqrt{3} x+4=0$ and $x-\sqrt{3} y=5$ are perpendicular to each other.
9. (a) Prove : $\cot 2 A+\tan A=\operatorname{cosec} 2 A$
(b) Prove: $2 \cos 105^{\circ} \cdot \cos 15^{\circ}+\frac{1}{2}=0$
(c) Solve: $\tan ^{2} \frac{\theta}{3}-\frac{2}{\sqrt{3}} \tan \frac{\theta}{3}+\frac{1}{2}=0$.
10. (a) If $\vec{a}+\vec{b}+\vec{c}=0,|\vec{a}|=6,|\vec{b}|=7$ and $|\vec{c}|=\sqrt{127}$, find the angle between $\vec{a}$ and $\vec{b}$.
(b) In $\triangle A B C, \overrightarrow{O A}=2 \vec{i}+3 \vec{j}, \overrightarrow{O B}=\vec{i}-2 \vec{j}$ and position vector of centroid $G$ of $\triangle A B C$ is $\overrightarrow{O G}=3 \vec{i}+4 \vec{j}$, then find $\overrightarrow{O C}$.
(c) In a data, the first quartile and the quartile deviation are 17.5 and 20 respectively. Find the third quartile and the co-officient of quartile deviation.

## Group"C"

$$
[11 \times 4=44]
$$

11. Solve: $3 x^{3}-13 x^{2}+16=0$
12. The sum of three numbers in AP is 18 . If 1,2 and 7 are added to them respectively, the numbers will be in G.P., then find the numbers.
13. If

$$
f(x)= \begin{cases}x+2 & \text { if } 1 \leq x<0 \\ 3 x-2 & \text { if } x \geq 2\end{cases}
$$

Then,
(a) Find $f(x)$ if $x=1.99$.
(b) Find $f(x)$ if $x=2.01$.
(c) Is $\lim _{x \rightarrow 2^{-}} f(x)=\lim _{x \rightarrow 2^{+}} f(x)$ ?
(d) Is $f(x)$ continuous at $x=2$ ?
14. Solve by matrix method: $4 x-\frac{9}{y}+11=0$ and $\frac{6}{y}-3 x=8$.
15. Find the single equation of the pair of straight lines passing through $(3,-1)$ and perpendicular to the pair of lines represented by $x^{2}-x y-2 y^{2}=0$.
16. Prove that:

$$
\sin ^{4} \frac{\pi^{c}}{8}+\sin ^{4} \frac{3 \pi^{c}}{8}+\sin ^{4} \frac{5 \pi^{c}}{8}+\sin ^{4} \frac{7 \pi^{c}}{8}=\frac{3}{2}
$$

17. If $A+B+C=\pi^{c}$ then prove that:

$$
\frac{\cos A}{\sin B \cdot \sin C}+\frac{\cos B}{\sin C \sin A}+\frac{\sin C}{\sin A \sin B}
$$

18. A ladder of length 20 feet is leaned on the top of a wall which makes an angle of $60^{\circ}$ with the ground. The ladder slides 7.32 feet below the top along the wall, find the new angle that the ladder makes with ground.
19. Find the inversion point of the given point $A(5,4)$ with respect to the circle $x^{2}+y^{2}-6 x-4 y+9=0$.
20. Find the mean deviation from median and its coefficient from the following frequency table.

| Marks | $0 \leq x<10$ | $10 \leq x<20$ | $20 \leq x<30$ | $30 \leq x<40$ | $40 \leq x<50$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Number of students | 5 | 2 | 9 | 2 | 2 |

