

Contents

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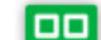
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Introduction	vii
Chapter 1 Arithmetic	1
1.1 Proportional Parts – Dividing Quantities in a Given Ratio	2
1.2 Approximation and Percentage Error	4
1.3 Income Tax	7
1.4 VAT: Value-Added Tax	12
1.5 Percentage Profit and Loss; Discounts (Allowed and Received)	15
1.6 Compound Interest: Loans and Investments.....	18
1.7 Depreciation (Reducing-Balance Method)	22
1.8 Average Rates of Change (with Respect to Time)	25
1.9 Costing: Materials, Labour and Wastage	27
1.10 Currency Exchange	32
1.11 Metric System – Imperial System	34
Chapter 2 Algebra I	42
2.1 Expressions	43
2.2 Substitution	44
2.3 Adding and Subtracting Terms	46
2.4 Multiplying Terms I	47
2.5 Multiplying Terms II	49
2.6 Algebraic Fractions I	50
2.7 Expanding and Re-Grouping Expressions	51
2.8 Factorising I	53
2.9 Factorising II	56
2.10 Simplifying Algebraic Fractions	59
2.11 Long Division in Algebra	60
2.12 Algebraic Fractions II	61
2.13 Solving Linear Equations	62
2.14 Solving Linear Equations with Fractions.....	65
2.15 Manipulation of Formulae	66
2.16 Solving Simultaneous Linear Equations by Elimination or Substitution	69
2.17 Solving Simultaneous Linear Equations Graphically	72
2.18 Linear Inequalities	74
2.19 Solving Inequalities.....	76
2.20 Writing Expressions	79
Chapter 3 Real Numbers	93
3.1 Natural Numbers	94
3.2 Factors, Multiples and Prime Factors	94
3.3 Integers	98
3.4 Rational Numbers	99
3.5 Decimals and Irrational Numbers	100
3.6 Scientific Notation	105
3.7 Order of Operations	107
Chapter 4 Indices	111
4.1 Numbers in Index Form	112
4.2 Laws 1–4 of Indices	112
4.3 Laws 5–9 of Indices	114
4.4 Equations with x as an Index	119
4.5 Surds	121
Chapter 5 Algebra II	124
5.1 Solving Quadratic Equations by Factorising	125
5.2 Solving Quadratic Equations by Formula	129
5.3 Solving Quadratic Equations Involving Fractions	132
5.4 Forming Quadratic Equations	134
5.5 Solving Simultaneous Equations: One Linear and One Non-Linear	136
5.6 Solving Problems that Lead to a Quadratic Equation	138
Chapter 6 Functions	149
6.1 Introduction	150
6.2 Composite Functions.	156
6.3 Linear Functions	158
6.4 Linear Functions Crossing the x -axis [$f(x) = 0$]	160
6.5 Quadratic Functions	161
6.6 Cubic Functions	166
6.7 Exponential Functions	170
6.8 Transformations of Quadratic Functions	175



Chapter 7 Number Patterns	187	Chapter 12 Probability	313	Chapter 16 Constructions, Transformations and Enlargements	479	Chapter 18 Co-ordinate Geometry: The Line	546
7.1 Patterns	188	12.1 Introducing Probability.....	314	16.1 Introduction	480	18.1 Distance Between Two Points on the xy-Plane	547
7.2 Arithmetic Sequences	191	12.2 Relative Frequency (Experimental Probability), Fairness and Expected Frequency	316	16.2 Junior Certificate Constructions	480	18.2 Midpoint of a Line Segment	550
7.3 The General Term of an Arithmetic Sequence	197	12.3 Theoretical Probability	322	16.3 Leaving Certificate Ordinary Level Constructions	485	18.3 Slope of a Line	552
7.4 Arithmetic Series.....	201	12.4 Set Theory and Probability	325	16.4 Transformations	493	18.4 The Equation of a Line	555
7.5 Some Non-Linear Sequences	206	12.5 Combined Events	332	16.5 Enlargements	498	18.5 Equations of the Form $y = mx + c$	557
Chapter 8 Complex Numbers	215	12.6 AND/OR: Multiple Events.....	338	16.6 Properties of Enlargements.....	505	18.6 Finding the Equation of a Line	560
8.1 Introduction	216	12.7 Bernoulli Trials	343	Chapter 17 Trigonometry	515	18.7 Intersecting Lines	561
8.2 Complex Numbers and the Argand Diagram	218	12.8 Expected Value	347	17.1 Right-Angled Triangles and Pythagoras' Theorem.....	516	18.8 Further Equations	564
8.3 Addition and Subtraction of Complex Numbers; Multiplication by a Real Number	220	Chapter 13 Statistics I.....	358	17.2 Right-Angled Triangles and the Trigonometric Ratios	518	18.9 Area of a Triangle	565
8.4 Modulus of a Complex Number	224	13.1 Statistics in Today's World	359	17.3 Finding the Length of a Side in a Right-Angled Triangle	521		
8.5 Multiplying Complex Numbers	225	13.2 Statistical Investigations	359	17.4 Using Trigonometry to Solve Practical Problems.....	523		
8.6 Conjugate of a Complex Number	228	13.3 Collecting Data	363	17.5 Special Angles $30^\circ, 45^\circ$ and 60°	525		
8.7 Dividing Complex Numbers	230	13.4 Frequency Tables	363	17.6 Area of a Triangle	528		
Chapter 9 Calculus	234	13.5 Graphing Data: Stem-and-Leaf Diagrams	365	17.7 The Unit Circle	530		
9.1 Calculus	235	13.6 Graphing Data: Histograms	369	17.8 Evaluating the Trigonometric Ratios of All Angles Between 0° and 360°	531		
9.2 Limits	235	13.7 Distribution of Data	370	17.9 The Sine Rule	534		
9.3 First Derivatives	238	13.8 Scatter Graphs and Correlation	376	17.10 The Cosine Rule	537		
9.4 Second Derivatives	241	Chapter 14 Statistics II	390	17.11 Length of an Arc and Area of a Sector	540		
9.5 Slopes of Tangents	242	14.1 Measures of Central Tendency: Mean, Mode and Median	391				
9.6 Increasing and Decreasing Functions	244	14.2 Deciding Which Average to Use	397				
9.7 Maxima and Minima	247	14.3 Measures of Variation 1: Range and Interquartile Range	399				
9.8 Maximum and Minimum Problems	249	14.4 Measures of Variation 2: Standard Deviation	404				
9.9 Rates of Change	252	14.5 The Normal Distribution and the Empirical Rule	407				
Chapter 10 Applied Measure.....	260	14.6 Sampling Variability	410				
10.1 Area and Perimeter of Triangles and Quadrilaterals	261	14.7 Margin of Error and Hypothesis Testing	414				
10.2 Circle	265	14.8 Misuses of Statistics	418				
10.3 Finding Dimensions When Given Area or Perimeter	269	Chapter 15 Geometry	424				
10.4 Rectangular Solids	272	15.1 Introduction	425				
10.5 Prisms	276	15.2 Basic Concepts	425				
10.6 Cylinders	278	15.3 Angles	427				
10.7 Right Circular Cones	280	15.4 Axioms	428				
10.8 Spheres	283	15.5 Theorem Terms	431				
10.9 Finding Dimensions When Given Volume or Surface Area	285	15.6 Angles and Lines	433				
10.10 Trapezoidal Rule	288	15.7 Triangles I: Angles and Sides	437				
Chapter 11 Counting and Permutations	297	15.8 Quadrilaterals	447				
11.1 Listing Outcomes	298	15.9 Area of a Triangle and Area of a Parallelogram	449				
11.2 The Fundamental Principle of Counting	302	15.10 Triangles II: Congruent Triangles	452				
11.3 Permutations	304	15.11 Triangles III: Ratios	455				
		15.12 Circles	463				
		15.13 Further Circles	467				

