## Why is SSA Not a Congruence Relationship?

## Use GeoGebra to explore what happens when attempting to construct a triangle given SSA

1. In GeoGebra, turn off the axes and grid.
2. Construct and measure segment $A B$.

3. With point $A$ as the endpoint, construct a ray making an acute angle with segment $A B$. (Notice how I place point C almost off the screen.) Measure angle BAC.

4. Construct segment $B D$. Segment $B D$ should not intersect ray $A C$. Measure segment $B D$.


IMPORTANT: Notice you have constructed side BD, side AB, and angle A---attempting to construct a triangle given SSA!
5. Exploration 1: Can a triangle be formed with the above dimensions?

It doesn't look like it is possible, but be sure construct a circle with center point B and radius BD. Using the Circle with Center through Point tool., click on center point $B$, then click on point $D$ to set the radius.


The distance from $B$ to any point on the circle is the same as the length of BD. With the given two sides and non-included angle (SSA) is a triangle possible?
6. Exploration 2: Drag point $D$ to change the length of segment BD.

Find a SSA situation where two triangles are possible. Draw and label a diagram below.

Find a SSA situation where exactly one triangle is possible. Draw and label a diagram below.

## Conclusion:

Complete the statement
SSA is not a triangle congruence relationship because
7. Exploration 3: Drag point $C$ so that angle BAC is an obtuse angle. Vary the length of BD and explore the possible triangles.


Conclusion:
In a given SSA relation with an obtuse triangle, how many triangles are possible? Why?

Does the result change if the given angle is a right angle?

